Global Calibration Based on Local Calibration for an Ultrasound Location Sensor*

Abstract—The ability to quickly construct a human activity observation system is required in order to conduct field research on human activities. The authors have developed an ultrasonic location system, which is a type of location sensing system for observing human activities. The present study attempts to establish a systematic method for quickly constructing an ultrasonic location system in various environments. A calibration function that can be used in various environments is one of the basic functions of the ultrasonic location system. In the present paper, we propose a new calibration method, “global calibration based on local calibration (GCLC),” for calibrating the 3D positions of ultrasonic receivers placed arbitrarily in a daily-use environment. The proposed method requires a relatively small number of transmitters and is independent of room size. In addition, we describe two constraints that can be used in conjunction with the GCLC method. The performance of the GCLC method was investigated in an experimental room (4.0×2.7 m), in which 80 ultrasonic receivers were attached to the ceiling. A portable system based partly on the proposed method is also presented herein.

Keywords—human activity observation, ultrasonic location sensor, calibration.

I. INTRODUCTION

Recently, human-centered information processing services have been attracting increasing attention. The goal of the present research is to establish a technique by which to recognize both human activity and the state in a living space. Therefore, it is necessary to observe human activity in real time and with high accuracy, without the presence of constraints that prevent natural human activities.

As a method for efficient and robust recognition of activities in a daily environment, the concept of object-based activity recognition has been proposed. The behavior of handling objects in an environment such as an office or home can be recognized based on the motion of the objects [1]. We have developed a three-dimensional (3D) ultrasonic location system as a fundamental system for robustly tracking objects and have verified that the observation of human activity based on object tracking is possible [2], [3]. However, like other location sensors, the developed ultrasonic location sensor has a disadvantage in that lack of portability makes it difficult to collect activity data in the various environments in which actual human activities occur.

In the present paper, we propose a rapid calibration method, “global calibration based on local calibration,” that enables users to quickly calibrate the positions of ultrasonic receivers of an ultrasonic location system and observe the system for field research on human activities.

II. RELATED WORK

Several types of ultrasonic location systems have been proposed. The Bat Ultrasonic Location System [4–7] developed by AT&T, and the MIT Cricket Indoor Location System [8] are well known. Although a calibration method using a robot [9] has been proposed, the required calibration device is too large for use in a number of environments. An auto calibration method was considered in the DOLPHIN system [10], which can calibrate the positions of receivers/transmitters using a small number of reference receivers/transmitters having known positions. However, the system has only been tested in narrow areas having dimensions of approximately 2.5 m × 2 m. Bristol University proposed another auto calibration method, in which the positions of n transmitters and m receivers can be calculated given n×m distance data among the transmitters and receivers and that the condition, 3(n+m)−6 < n·m, is satisfied [11]. However, the scalability of this method is limited.

In contrast, the present study proposes and examines a new calibration method, “global calibration based on local calibration,” that requires a relatively small number of transmitters and is independent of room size. Using the proposed method, the calibration problem becomes similar to a fitting problem in object modeling with multiple range images [12], [13] after local calibration.

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A. Proposal of a rapid calibration method

In the present paper, in addition to the "global calibration based on local calibration (GCLC)" method, we propose a new calibration method that can be used in conjunction with the GCLC method, as described below.

The procedure for GCLC is described below.

1. Move the calibration device to multiple positions (A, B, and C in Fig. 1).
2. Calculate the positions of the receivers in a local coordinate system, with the local origin set at the position of the calibration system.
3. Select receivers for which the positions can be calculated from more than two calibration system positions.
4. Select a global coordinate system from among the local coordinate systems and calculate the positions of the calibration device in the global coordinate system using the selected receivers.
5. Calculate the receiver positions using the positions calculated in Step 2 and the transformation matrices calculated in Step 4.

Steps 2 and 4 are described in detail in the following.

B. Linear method for rapid calibration

1) Calculating the 3D positions of receivers in a local coordinate system based on distance data (Step 2):

The receiver position \((x,y,z)\) is calculated by a multilateration algorithm, such as that used in the Global Positioning System [14]. The multilateration algorithm has been proposed in the field of aerospace [15], [16]. The present paper briefly describes a multilateration algorithm based on simultaneous linear equations [2] that is applicable to a more general case, in which multiple ultrasonic receivers are placed in arbitrary positions. This is explained in detail below.

Here, \(l_1, l_2, \ldots, l_4\) denote the distances from the ultrasonic receiver at \((x,y,z)\) to the \(i\)th ultrasonic transmitter placed at \((x_i, y_i, z_i)\). Using the spherical equations, we obtain simultaneous linear equations for the intersecting planes between the spheres as

\[
AP = B,
\]

where \(P = \begin{pmatrix} x \\ y \\ z \end{pmatrix}\),

\[
A = \begin{pmatrix}
2(x_2 - x_1) & 2(y_2 - y_1) & 2(z_2 - z_1) \\
2(x_3 - x_1) & 2(y_3 - y_1) & 2(z_3 - z_1) \\
2(x_4 - x_1) & 2(y_4 - y_1) & 2(z_4 - z_1) \\
\end{pmatrix},
\]

\[
B = \begin{pmatrix}
l_1^2 - x_1^2 - y_1^2 - z_1^2 \\
l_2^2 - x_2^2 - y_2^2 - z_2^2 \\
l_3^2 - x_3^2 - y_3^2 - z_3^2 \\
l_4^2 - x_4^2 - y_4^2 - z_4^2 \\
\end{pmatrix}.
\]

For the case of four or more transmitters that are not coplanar, the rank of \(A\) becomes 3. The position \((x,y,z)\) can be calculated by the least squares method as

\[
P = (A^T A)^{-1} A^T B.
\]

This method calculates position by solving plane equations derived from the equations of intersecting spheres. Reference [2] presents a detailed description for the case in which the rank of \(A\) is 2.

2) Calculating the positions of the calibration device in the global coordinate system (Step 4):

The error function \(E\) can be defined as follows:

\[
E = \sum_{i=0}^{n} \sum_{j=i+1}^{n} ||M_i P_i^{(i,j)} - M_i P_j^{(i,j)}||^2,
\]

where \(M_i\) is the transformation matrix from the local coordinate system \(i\) to the global coordinate system, and \(P_i^{(i,j)}\) denotes points in the local coordinate system \(j\) for the case in which the points can be calculated in both local coordinate systems \(i\) and \(j\).

If we select the local coordinate system 0 as the global coordinate system, \(M_0\) becomes an identity matrix. From
Eq. (7), we can obtain simultaneous linear equations and calculate $M_i$ using Eq. (8),

$$\begin{bmatrix} M_1 & M_2 & \cdots & M_n \end{bmatrix} = \begin{bmatrix} p_0^{(0,1)} & p_0^{(0,2)} & \cdots & p_0^{(0,n)} \\ p_1^{(0,1)} & p_1^{(0,2)} & \cdots & p_1^{(0,n)} \\ \vdots & \vdots & \ddots & \vdots \\ p_n^{(0,1)} & p_n^{(0,2)} & \cdots & p_n^{(0,n)} \end{bmatrix} \times \begin{bmatrix} -p_1^{(1,1)} & -p_1^{(1,2)} & \cdots & -p_1^{(1,n)} \\ -p_2^{(1,1)} & -p_2^{(1,2)} & \cdots & -p_2^{(1,n)} \\ \vdots & \vdots & \ddots & \vdots \\ -p_n^{(1,1)} & -p_n^{(1,2)} & \cdots & -p_n^{(1,n)} \end{bmatrix}^{-1}$$

$$\sum_{i=0}^{n-1} p_i^{(1,1)} \left( \sum_{j=0}^{n-1} p_j^{(2,1)} \right) - \sum_{i=0}^{n-1} p_i^{(1,2)} \left( \sum_{j=0}^{n-1} p_j^{(2,2)} \right) - \sum_{i=0}^{n-1} p_i^{(1,n)} \left( \sum_{j=0}^{n-1} p_j^{(2,n)} \right) = -\lambda F(M_3),$$

where $\lambda$ denotes a Lagrange’s undecided multiplier. By solving this equation, we can obtain the following equations:

$$\begin{bmatrix} M_2 & M_3 \end{bmatrix} = \begin{bmatrix} p_0^{(0,1)} & p_0^{(0,2)} \\ p_1^{(0,1)} & p_1^{(0,2)} \\ \vdots & \vdots \\ p_n^{(0,1)} & p_n^{(0,2)} \end{bmatrix} \times \begin{bmatrix} -p_1^{(1,1)} & -p_1^{(1,2)} \\ -p_2^{(1,1)} & -p_2^{(1,2)} \\ \vdots & \vdots \\ -p_n^{(1,1)} & -p_n^{(1,2)} \end{bmatrix}^{-1} \lambda F(M_3),$$

$$\sum_{i=0}^{n-1} p_i^{(1,1)} \left( \sum_{j=0}^{n-1} p_j^{(2,1)} \right) - \sum_{i=0}^{n-1} p_i^{(1,2)} \left( \sum_{j=0}^{n-1} p_j^{(2,2)} \right) - \sum_{i=0}^{n-1} p_i^{(1,n)} \left( \sum_{j=0}^{n-1} p_j^{(2,n)} \right) = -\lambda F(M_3).$$

By substituting $M_3$ into Eq. (10), we can solve $\lambda$ and eliminate it from Eq. (11).

The general case of the GCLC method with multiple boundary constraints is as follows:

$$\begin{bmatrix} M_1 & M_2 & \cdots & M_n \end{bmatrix} = \begin{bmatrix} p_0^{(0,1)} & p_0^{(0,2)} & \cdots & p_0^{(0,n)} \\ p_1^{(0,1)} & p_1^{(0,2)} & \cdots & p_1^{(0,n)} \\ \vdots & \vdots & \ddots & \vdots \\ p_n^{(0,1)} & p_n^{(0,2)} & \cdots & p_n^{(0,n)} \end{bmatrix} \times \begin{bmatrix} -p_1^{(1,1)} & -p_1^{(1,2)} & \cdots & -p_1^{(1,n)} \\ -p_2^{(1,1)} & -p_2^{(1,2)} & \cdots & -p_2^{(1,n)} \\ \vdots & \vdots & \ddots & \vdots \\ -p_n^{(1,1)} & -p_n^{(1,2)} & \cdots & -p_n^{(1,n)} \end{bmatrix}^{-1} \lambda F(M_3),$$

where $\lambda_{i,j}$, $n_{1,j}$, and $P_{1,j}$ denote the j-th undecided multiplier, the j-th constraint vector, and the j-th constrained point in the i-th local coordinate system, respectively. In this case, the boundary constraints are as follows:

$$F_{i,j} = (M_1 P_{1,j} - P_{0,0}) \cdot n + l_0 - l_1 = 0,$$

where $\Delta l_{i,j}$ denotes a distance constraint. The above GCLC method with boundary constraints is applicable to, for example, the case in which more complex boundary conditions exist, as shown in Fig. 3.

**D. Consideration of ultrasonic damping**

1. **Error due to ultrasonic damping**: The authors discovered a phenomenon whereby the measured distance between receivers and transmitters appears longer than...
the actual distance due to ultrasonic damping. This phenomenon causes an increase in the error. The damping is caused by the directivities of the transmitter and the receiver. This section describes a method that considers the directivities in order to reduce this effect.

The newly developed ultrasonic location system measures the distance from the time-of-flight of the ultrasonic pulse. The time at which the ultrasonic wave exceeds the threshold is the arrival time of the ultrasonic pulse at the receiver, as shown in Fig. 4. However, in the case of damping of the ultrasonic wave, due to the effects of directivity and distance, the error of the measured distance increases as a result of the delay in the ultrasonic pulse arrival time expressed by $\Delta T$.

2) Approach to the damping problem: There are two approaches to this problem: a hardware approach and a software approach. In the hardware approach, the highest point of the ultrasonic wave, for example, can be assumed to be the ultrasonic pulse arrival time, as determined by sampling and analyzing the ultrasonic wave, which requires expensive equipment. Therefore, in the present paper, we consider the software approach.

3) Method for dealing with the damping problem: The distance between the receivers and transmitters is

$$|Pr_i - Pt_j| = L_{ij},$$

(14)

where $Pr_i$ are the positions of the receivers, $Pt_j$ are the positions of the transmitters, and $L_{ij}$ are the actual distances. The ultrasonically measured distances $L_{m,ij}$ are longer than the actual distances $L_{ij}$. The actual distances $L_{ij}$ are described by

$$L_{ij} = L_{m,ij} - \Delta L_{ij},$$

(15)

where $\Delta L_{ij}$ is the error of the distance.

IV. EXPERIMENTS

A. System configuration

Figure 7 shows the system configuration for the proposed 3D ultrasonic tag system. The system consists of an ultrasonic receiving section, an ultrasonic transmitting section, a time-of-flight measurement section, a network section, and a personal computer. The ultrasonic receiving section receives ultrasonic pulses emitted from the ultrasonic transmitter and amplifies the received signal. The time-of-flight measurement section records the travel time of the signal from transmission to reception. The network section synchronizes the system and collects time-of-flight data from the ultrasonic receiving section. The positions of objects are calculated based on more than three time-of-flight measurements.

B. Experimental results

1) Method for error evaluation: Errors are defined as the distances between the calculated receiver positions and the true receiver positions and are denoted by $e_1, e_2, \ldots$. Here,

$$\Delta L_{ij} = -61.323 \cos \theta_{ij} - 75.622 \cos \phi_{ij} + 131.662$$

(16)

was obtained experimentally.
The average error is defined by

$$E = \frac{1}{n} \sum_{i=1}^{n} e_i.$$  \hspace{1cm} (17)

2) Accuracy evaluation: Calibration was performed in a room (4.0×4.0×2.5 m) having 80 ultrasonic receivers embedded in the ceiling. Figure 8 shows the experimental results obtained using the GCLC method without any constraints. The authors performed calibration at 16 points in the room. Seventy-six receivers were calculated. In the figure, the red spheres indicate calculated receiver positions, the black crosses indicate the true receiver positions, and the blue spheres indicate the positions of the calibration device. Figure 9 shows the experimental results for the GCLC method considering directivities. Seventy-six receivers were calculated. Table I shows the average error $E$, maximum error, and minimum error for these methods. The above results show that using the GCLC method we can calibrate the position of receivers placed in a space of average room size and that the error can be reduced significantly by considering directivity.

Another calibration was performed in a rectangular space (1.0×4.5) having a longitudinal length that is much longer than its lateral length. Seventy-six ultrasonic receivers were embedded in the space. Figure 10 shows the experimental results obtained using the GCLC method without any constraints. Seventy-five receivers were calculated. Figure 11 shows the experimental results obtained using the GCLC method directivity consideration and a boundary constraint. Table II shows the average error $E$, maximum error, and minimum error for these methods. The above results show that with the GCLC method with directivity consideration and boundary constraint has a significantly reduced error.

<table>
<thead>
<tr>
<th>Method</th>
<th>Ave. error</th>
<th>Max. error</th>
<th>Min. error</th>
</tr>
</thead>
<tbody>
<tr>
<td>GCLC</td>
<td>195 mm</td>
<td>399 mm</td>
<td>66 mm</td>
</tr>
<tr>
<td>GCLC with directivity consideration</td>
<td>75 mm</td>
<td>276 mm</td>
<td>9 mm</td>
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</tbody>
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Table I: Errors (mm) of the proposed method for the case of a square-like space

<table>
<thead>
<tr>
<th>Method</th>
<th>Ave. error</th>
<th>Max. error</th>
<th>Min. error</th>
</tr>
</thead>
<tbody>
<tr>
<td>GCLC</td>
<td>236 mm</td>
<td>689 mm</td>
<td>17 mm</td>
</tr>
<tr>
<td>GCLC with directivity consideration and boundary constraint</td>
<td>51 mm</td>
<td>121 mm</td>
<td>10 mm</td>
</tr>
</tbody>
</table>

Table II: Errors (mm) of the proposed method for the case of a rectangular space having a longitudinal length that is much longer than its lateral length
V. ADVANTAGES OF THE GCLC METHOD
The advantages of the GCLC method are listed below.

- The method requires a relatively small number of transmitters, at least three transmitters, so that the user can calibrate the ultrasonic location system using a small calibrating device having at least three transmitters.
- The method can calibrate the positions of the receivers independent of room size.
- The error can be reduced by considering the directivity constraint. The constraint is useful for cases in which the ultrasonic location system adopts a method in which the time-of-flight is detected by thresholding the ultrasonic pulse.
- The error can be reduced by considering the boundary constraint. The constraint is useful for cases in which the receivers to be calibrated are placed in a rectangular space having a longitudinal length that is much greater than the lateral length, such as a long corridor.

VI. REALIZED ULTRASONIC PORTABLE 3D TAG SYSTEM
The GCLC method enables a portable ultrasonic 3D tag system. Figure 12 shows a portable ultrasonic 3D tag system, which consists of a case, tags, receivers, and a calibration device. The portable system enables measurement of human activities by quickly installing and calibrating the system on-site, at the location where the activities actually occur.

![Developed portable ultrasonic 3D tag system](image)

Fig. 12. Developed portable ultrasonic 3D tag system

VII. CONCLUSION
In the present paper, we proposed a new calibration method, “global calibration based on local calibration (GCLC)”, for an ultrasonic location system so that users can quickly calibrate a system and observe human activity in various environments where the activities actually occur. One of the advantages of the GCLC method is the requirement for a relatively small number of transmitters. In addition, the GCLC method is not dependent on room size. We also described two constraints that can be used in conjunction with the GCLC method: the directivity constraint and the boundary constraint.

In addition, a portable ultrasonic location sensor based on the proposed method was realized. The portable system allows human activities to be measured in the area where the activities actually occur with quick installation and calibration.

Further studies will examine the refinement of the method in order to measure the 3D positions with higher accuracy, systematization of calibration methods, and the use of the portable 3D ultrasonic tag system in a living space.

REFERENCES