

cheat sheet finset.v (SSREFLECT v1.5)

ssrfun.v naming conventions

K cancel  
 LR move an op from the lhs of a rel to the rhs  
 RL move an op from the rhs to the lhs

ssrfun.v definitions

```

injective f      forall x1 x2, f x1 = f x2 -> x1 = x2
cancel f g      g (f x) = x
involutive f    cancel f f
left_injective op injective (op^^ x)
right_injective op injective (op y)
left_id e op    op e x = x
right_id e op  op x e = x
left_zero z op op z x = z
right_commutative op op (op x y) z = op (op x z) y
right_zero z op op x z = z
left_commutative op op x (op y z) = op y (op x z)
left_distributive op add op (add x y) z = add (op x z) (op y z)
right_distributive op add op x (add y z) = add (op x y) (op x z)
left_loop inv op cancel (op x) (op (inv x))
self_inverse e op op x x = e
commutative op  op x y = op y x
idempotent op  op x x = x
associative op  op x (op y z) = op (op x y) z
    
```

ssrbool.v naming conventions

A associativity  
 AC right commutativity  
 b a boolean argument  
 C commutativity/complement  
 D predicate difference  
 E elimination  
 F/f boolean false  
 T/t boolean truth  
 U predicate union

finset.v naming conventions

0 the empty set  
 T the full set  
 1 singleton set  
 C complement  
 U union  
 I intersection  
 D difference

set\_scope

```

<math>\times</math> set0
A :|: B setU
a |: A [set a] :|: A
A :&: B setI
~: A setC A
A :\: B setD A B
A :\ a A :\: [set a]
f @~-1: A preimset f (mem A)
f @: A imset f (mem A)
f @2: ( A , B ) imset2 f (mem A) (fun _ =>mem B)
    
```

bool\_scope

```

<math>\emptyset</math> a \in A see ssrbool.v a ∈ A
A ∪ B A \subset B see fintype.v A ⊆ B
{a} ∪ A [disjoint A & B] see fintype.v A ∩ B = ∅
A ∩ B
AC
A \ B
A \ {a}
f-1(A)
f(A)
f(A, B)
    
```

```

setP A =i B <-> A = B
in_set0 x \in set0 = false
subset0 (A \subset set0) = (A == set0)
in_set1 (x \in [set a]) = (x == a)
in_setD1 (x \in A :\ b) = (x != b) && (x \in A)
in_setU (x \in A :|: B) = (x \in A) || (x \in B)
in_setC (x \in ~: A) = (x \notin A)
(NB: inE: in_set0, in_set1, in_setD1, in_setU, in_setC, etc.)
setUC A :|: B = B :|: A
setIC A :&: B = B :&: A
setKI A :|: (B :&: A) = A
setCI ~: (A :&: B) = ~: A :|: ~: B
setCK involutive (@setC T)
setD0 A :\: set0 =A
cardsE #|[set x in pA]| = #|pA| (NB: cardE : #|A| = size (enum A) in fintype.v)
cards0 #|@set0 T| = 0 (NB: card0 : #|pred0 T|=0 in fintype.v)
cards_eq0 (#|A| == 0) = (A == set0)
cardsU #|A :|: B| = #|A| + #|B| - #|A :&: B|
cardsT #|[set: T]| = #|T| (NB: cardT : #|T| = size (enum T) in fintype.v)
setOPn reflect (exists x, x \in A) (A != set0)
subsetI1 A :&: B \subset A
subsetUr B \subset A :|: B
subsetI (A \subset B :&: C) = (A \subset B) && (A \subset C)
setI_eq0 (A :&: B == set0) = [disjoint A & B]
imsetP reflect (exists2 x, in_mem x D & y = f x) (y \in imset f D)
card_imset injective f ->#|f @: D|=#|D|
    
```

Section Partitions

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cover P  $\bigcup_{B \in P} B$ 
trivIset P  $\sum_{B \in P} |B| = |cover(P)|$ 
see also bigop_doc.pdf
    
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