

重力モデル計算メモ (3)

<物理探査ハンドブックより>

重力異常の計算式として広く知られた方法に Talwani et al.(1959)がある。

断面 OPQ の Zi (単位密度重力値 / 2 G) は

$$Z_i = \frac{(x_{i+1} - x_i)(x_i z_{i+1} - x_{i+1} z_i)}{(x_{i+1} - x_i)^2 + (z_{i+1} - z_i)^2} \left\{ \tan^{-1} \frac{z_i}{x_i} - \tan^{-1} \frac{z_{i+1}}{x_{i+1}} + \frac{1}{2} \frac{z_{i+1} - z_i}{x_{i+1} - x_i} \ln \left(\frac{x_{i+1}^2 + z_{i+1}^2}{x_i^2 + z_i^2} \right) \right\}$$

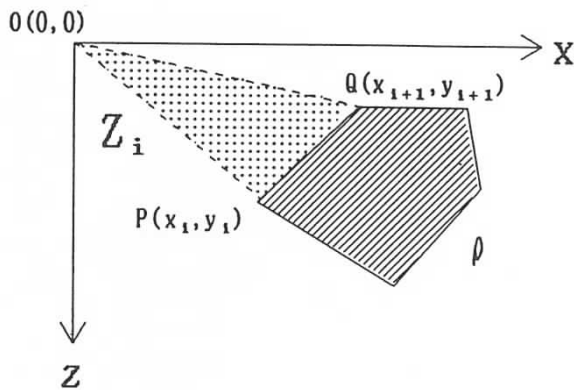


図8.20 2次元の多角形 (密度 ρ) モデル

図 8.20 に示す多角形 (密度 ρ) の重力値 (Δg) は

$$\Delta g = 2G\rho \sum_{i=1}^n Z_i$$

($n+1$ は 1 に一致させて閉塞させる)

解析断面に直交する範囲が有限な場合の r - θ 座標による表現を示す (Komazawa,1995)。

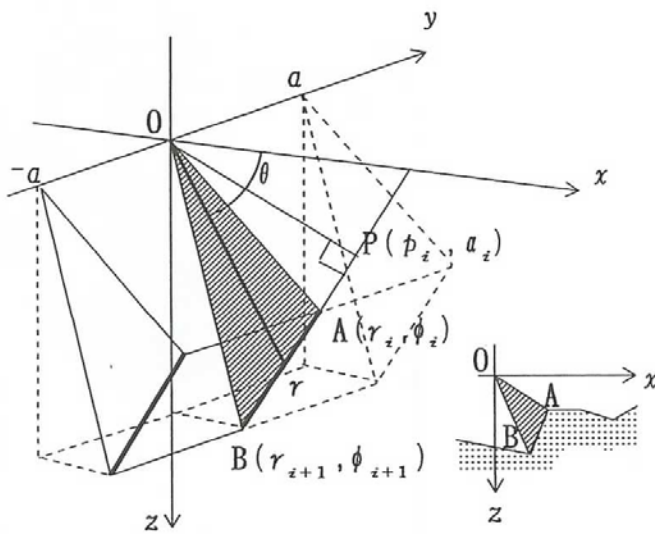


図8.21 2.5次元解析の計算断面モデル

図 8.21 より幾何学関係は

$$p_i = r_i \cos(\phi_i - \alpha_i) = r_{i+1} \cos(\phi_{i+1} - \alpha_{i+1}) = r \cos(\theta - \alpha_i)$$

$$r = r_i \cos(\phi_i - \alpha_i) / \cos(\theta - \alpha_i)$$

断面線から端の長さが a である有限 2 次元モデルの計算式について考慮する。

$$\int_0^a \frac{dy}{(x^2 + y^2 + z^2)^{3/2}} = \frac{1}{x^2 + z^2} \frac{a}{\sqrt{x^2 + z^2 + a^2}}$$

より

$$Z_i = \iint_S \frac{a}{\sqrt{x^2 + z^2 + a^2}} \frac{z dx dy}{x^2 + z^2}$$

$$= \iint_S \frac{a}{\sqrt{r^2 + a^2}} \sin \theta dr d\theta$$

$$= \int_{\phi_i}^{\phi_{i+1}} a \ln \left(\frac{r}{a} + \sqrt{1 + \frac{r^2}{a^2}} \right) \sin \theta d\theta$$

ここで $a \rightarrow \infty$ とすれば

$$Z_i = \int_{\phi_i}^{\phi_{i+1}} r(\theta) \sin \theta d\theta = r_i \cos(\phi_i - \alpha_i) \left\{ (\phi_{i+1} - \phi_i) \sin \alpha_i - \cos \alpha_i \ln \left| \frac{\cos(\phi_{i+1} - \alpha_i)}{\cos(\phi_i - \alpha_i)} \right| \right\}$$

ただし

$$\alpha_i = \tan^{-1} \left(\frac{y_{i+1} - y_i}{x_{i+1} - x_i} \right) - \frac{\pi}{2}$$

Komazawa(1995)より 2 次元多層モデルの計算プログラム angmdl2.f

入力ファイル

重力データ gravdata.txt

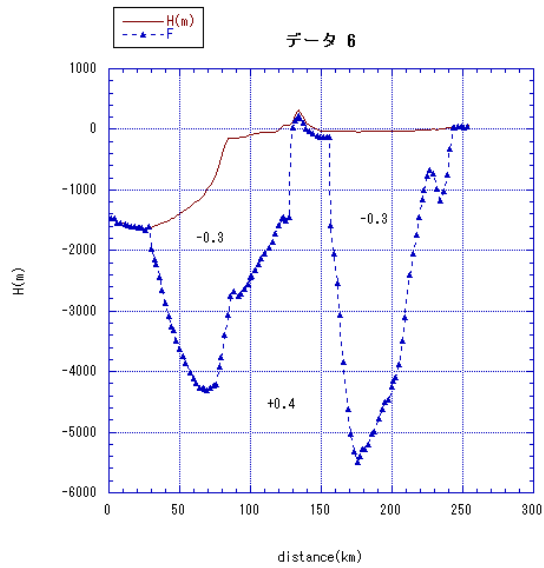
119 ← データ数

1 1.73774 -1473.8 12.426 ← NN, XD(km), H(m), G-obs(mgal)

2 3.96276 -1468.3 10.861

3 6.19107 -1537.8 7.485

入力モデルは下図。



モデルパラメーターmodel.txt

3 2 1 ← lay (層の数)、ipol (トレンドの次数)、it (1=トレンドを計算する、0=計算しない)

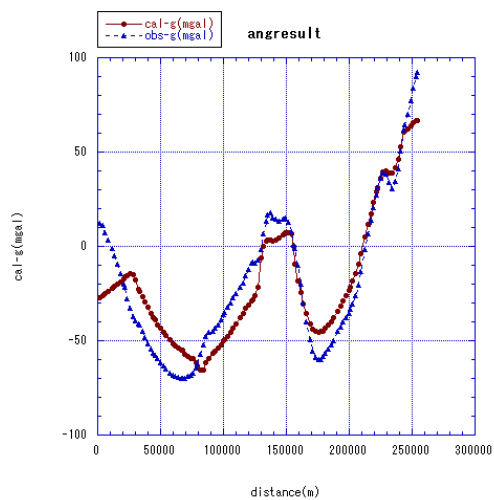
118 0.4 1 5000 ← lpnt (エッジの数)、dn1 (密度差 mgal)、lex (1=オープン層、0=クローズ層; p(1)=p(end)であるような層をクローズ層という)、aa (層の幅m)

1 1.73774 -1473.8 ← NN, XD(km),H(m)

.....

2222 ← ik (2222=層の終わり、3333=ファイルの終わり)

計算結果



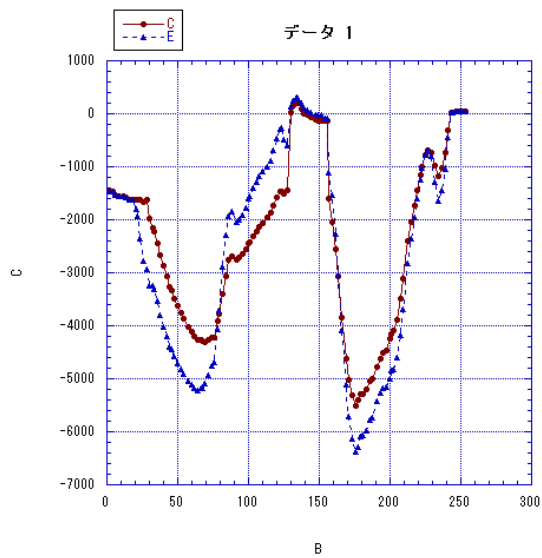
ここから同様にモデルを微修正する。

$$\Delta H(m) = (\text{calc}g - \text{obs}g) (\text{mgal}) / (2 * 3.14 * 6.67 * 0.001 * \Delta \rho (\text{mgal}))$$

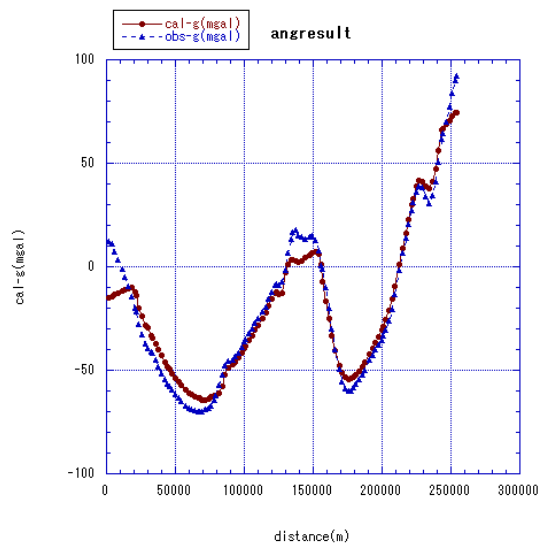
を計算し、修正したい箇所に加える。ここで修正値が地形データより大きくなったら、その部分は地形データで置き換える。

Blakely の計算式を使ったモデルと少々違うのは当然のこと。

C→E へモデルを修正。



計算結果



両端の値はモデルの打ち切り誤差の影響なので、ここでは無視する。
更に修正を加える場合もあるし、この辺で良しとする場合もある。

プログラム

```
c      2-D Gravity Model program
c
c          ver.1    with observed data
c          original Komazawa-san
c          modified RIE Morijiri
c
c      - ang -
c          common /ag/ag(500)
c          common /xa/xa(500)/ya/ya(500)
c          common /xb/xb(500)/yb/yb(500)
c
c      - iteration -
c          common /gc/gc(500)/go/go(500)
c          common /to/to(500)/rg/rg(500)
c          common /xo/xo(500)/yo/h(500)
c          common /xp/xp(500)/yp/d(500)
c          common /xc/xc(500)/yc/dc(500)
c          common /ite/iobs,den,ipol,it
c
c      - layers data -
c          common /gl/gl(500,20)
c          common /xl/xl(500,20)/yl/yl(500,20)
c          common /lay/lay,lpnt(20),dnl(20),lex(20),ldpl(20),aa(20)
c
c      -----
c          data i2,i3/2222,3333/
c
c          open(10,file='I:\¥grav-DB¥model.txt',status='old')
c          open(15,file='I:\¥grav-DB¥gravdata.txt',status='old')
c          open(30,file='I:\¥grav-DB¥angresult.txt')
c
c      -----  obs.pnt. input  -----
c          read(15,*) iobs
c          m = 0
c          do 2 k=1, iobs
c              read(15,*) nn,xd,hei,gobs
c              m = m + 1
```

```

        xo(m) = xd*1000
        h(m)  = hei
        go(m) = gobs
2 continue
        mw=m
        close(15)
c
c   write(6,616)
c 616 format(1h , '--- distance from origin ---')
c   write(6,603) (xo(i),i=1,mw)
c   write(6,617)
c 617 format(1h , '--- height data ---')
c   write(6,603) (h(i),i=1,mw)
c   write(6,618)
c 618 format(1h , '--- observed gravity data ---')
c   write(6,603) (go(i),i=1,mw)
c   if( mw .ne. iobs ) go to 3
c   -----
c   read(10,*) lay,ipol,it
c   -----
c   write(6,601) iobs,lay,ipol,it
601 format(1h , 'iobs =',i5,5x, 'lay no. =',i5/
&       1h , 'ipol=',i2,5x, 'it =',i2)
c
c   ++++++
c   +++ calculation of layers structure +++
c   ++++++
c   *****
c   *   l   : layer's no.   *
c   *   lpnt: layer's points *
c   *   dnl : layer's density *
c   *****
c   if( lay .le. 0 ) go to 4
        l = 0
11   l = l + 1
c   <---< l-th layer data input <---<

```

```

read(10,*) lpnt(l),dnl(l),lex(l),aa(l)
  k = 0
c   >----->
do 12 i=1,lpnt(l)
  read(10,*) ii,xd,yd
  k = k + 1
  xl(k,l) = xd*1000
  yl(k,l) = yd
12 continue
c   <-----<
read(10,*) inum
write(6,*) '83-inum   ;',inum
  if( k .ne. lpnt(l) ) go to 5
  if( inum .eq. i2 ) go to 11
  if( l .ne. lay ) go to 4
  if( inum .eq. i3 ) go to 13
c   >---> l-th layer data input >--->
c   --- calculation of layers structure --->
13 continue
  do 21 l=1,lay
  lw = 10*( lpnt(l)/10 + 1 )
  write(6,619) l,dnl(l),lpnt(l),lex(l),aa(l)
619 format(1h0,10x,'***',i2,'-th layer ***',5x,'den =',f6.2,5x,
  & 'lpnt =',i3,5x,'lex =',i2,5x,'width =',f8.1/)
  write(6,606)
606 format(1h ,10x,'--- x(layer boundary) ---')
  write(6,603) (xl(i,l),i=1,lw)
  write(6,607)
607 format(1h ,10x,'--- y(layer boundary) ---')
  write(6,603) (yl(i,l),i=1,lw)
c   -----
  jpnt = lpnt(l)
  dnj = dnl(l)
  jex = lex(l)
c   jdpl = ldpl(l)
  aaj = aa(l)

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c      -----
      call chg1(xo,xa)
      call chg1(h,ya)
      call chg2(xl,l,xb)
      call chg2(yl,l,yb)
c      --- l-th layer's values --->
      call angleg(iobs,jpnt,dnj,jex,aaj)
c      <-----
      call chg3(ag,gl,l)
c      -----
      write(6,608)
608 format(1h ,10x,'--- g(calculated values) ---')
      write(6,603) (gl(i,l),i=1,mw)
      21 continue
c <--- calculation of layers structure ---
      do 15 i=1,iobs
          gc(i) = 0.
          do 14 l=1,lay
              gc(i) = gc(i) + gl(i,l)
          14 continue
      15 continue
      write(6,615)
      write(6,603) (gc(i),i=1,mw)
          go to 8
c      >----->
      3 write(6,620)
620 format(1h , '***** observed point(iobs) is error. *****')
      go to 310
      4 write(6,621)
621 format(1h , '***** layers number is error. *****')
      go to 310
      5 write(6,622) l
622 format(1h , '*****',i2,'-th layer points is error. *****')
      go to 310
c      <-----<
      8 continue

```



```

c -----
  call trend(ipol,it)
  call stadev(iobs,gc,go)
  write(6,615)
615 format(1h0,5x,'----- calculated gravity -----')
  write(6,603) (gc(i),i=1,mw)
c -----
  do 88 i=1,mw
  write(30,*) xo(i),gc(i),go(i)
88 continue
  close(30)
c ++++++
310 continue
600 format(1h0,5x,'-----'/
/      1h ,5x,'line name = ',3a4/
/      1h ,5x,'-----')
603 format(1h ,10f10.2)
605 format(1h ,11x,' mean depth = ',f10.2)
609 format(1h ,10(5x,5h-----))
  stop
  end
c *****
c  angleg * two dimensional analysis *
c        * by angle integration *
c *****
  subroutine angleg(iobs,ipnt,den,iex,aa)
  common /ag/ag(500)
  common /xa/xo(500)/ya/yo(500)
  common /xb/xp(500)/yb/yp(500)
c -----  exerpotation of structure  ----
  call kyoku(xo,iobs,omin,omax)
  call kyoku(xp,ipnt,pmin,pmax)
  call kyoku(yo,iobs,ymin,ymax)
  xs = amin1(omin,pmin)
  xe = amax1(omax,pmax)
  rng = xe - xs

```

```

        m = iobs
        n = ipnt + 6
        if( iex .eq. 0 )  n = ipnt
        dm = 0.
          do 10 i=1,ipnt
            dm = dm + yp(i)
1      continue
        dmean = dm/float(ipnt)
        dpl=amin1(dmean,ymin)
c      if( idpl .eq. 0 )  dpl = 0.
c      if( idpl .ne. 0 )  dpl = dmean
        write(6,601) iobs,ipnt,den,xs,xr,ng,dmean
601 format(1h0,15x,'angtal : iobs =',i4,3x,
&          'ipnt =',i4,5x,'den =',f6.2/
& 1h ,15x,'      : xs =',e12.4,3x,'xe =',e12.4,5x,
&          'rng =',e12.4/
& 1h ,15x,'      : mean depth = ',e12.4)
        xs = xp(1)
        ys = yp(1)
        xe = xp(ipnt)
        ye = yp(ipnt)
        xp(ipnt+1) = xe + 0.5*rng
        xp(ipnt+6) = xs - 0.5*rng
        xp(ipnt+2) = xe + rng
        xp(ipnt+5) = xs - rng
        xp(ipnt+3) = xe + 4.*rng
        xp(ipnt+4) = xs - 4.*rng
        yp(ipnt+1) = ye
        yp(ipnt+6) = ys
        yp(ipnt+2) = 0.6*ye + 0.4*dpl
        yp(ipnt+5) = 0.6*ys + 0.4*dpl
        yp(ipnt+3) = dpl
        yp(ipnt+4) = dpl
c      -----
c      ----- calculation of obs.pnt -----
        do 10 i=1,m

```

```

at1 = 0.
x0 = xo(i)
y0 = yo(i)
  do 20 j=1,n
x1 = xp(j)
y1 = yp(j)
k = j + 1
if( j .eq. n ) k = 1
x2 = xp(k)
y2 = yp(k)
if( aa .eq. 0. .or. aa .eq. 99999. ) go to 11
at1 = at1 + den*sal(x0,y0,x1,y1,x2,y2,aa)
  go to 20
11 at1 = at1 + den*tal(x0,y0,x1,y1,x2,y2)
20 continue
  ag(i) = at1
10 continue
c -----
  return
  end
c      *-*-*-*-*-*-*-*-*-*-*
  function tal(x0,y0,x1,y1,x2,y2)
  pai = 3.141593
  yen = 2.*pai
  gg = 6.670e-3
  rr1 = (x1-x0)**2 + (y1-y0)**2
  rr2 = (x2-x0)**2 + (y2-y0)**2
  if( rr1 .eq. 0. .or. rr2 .eq. 0. ) go to 100
  r1 = sqrt(rr1)
  r2 = sqrt(rr2)
  pl = (x1-x0)*(y2-y0) - (x2-x0)*(y1-y0)
  sg = 1.0
  if( pl .lt. 0. ) sg = -1.
  qh = phase(x2-x1,y2-y1) - 0.5*pai
  ph1 = phase(x1-x0,y1-y0)
  ph2 = phase(x2-x0,y2-y0)

```

```

phm = abs(ph2-ph1)
if( phm .eq. 0.) go to 100
if( phm .gt. pai .and. phm .le. yen ) phm = yen - phm
  c1 = cos(ph1-qh)
  c2 = cos(ph2-qh)
  if( c1 .eq. 0.) go to 100
  ab = abs(c2/c1)
  alg = alog(ab)
  tt = r1*c1*( sg*phm*sin(qh) - alg*cos(qh) )
  go to 200
100 tt = 0.
200 continue
  tal = 2.0 * tt * gg
  return
end
c      *-*-*-*-*-*-*-*-*-*-*-*
      function sal(x0,y0,x1,y1,x2,y2,aa)
      pai = 3.141593
      yen = 2.*pai
      gg = 6.670e-3
      tt = 0.
      rr1 = (x1-x0)**2 + (y1-y0)**2
      rr2 = (x2-x0)**2 + (y2-y0)**2
      if( rr1.eq.0. .or. rr2.eq.0. ) go to 100
      r1 = sqrt(rr1)
      ph1 = phase(x1-x0,y1-y0)
      ph2 = phase(x2-x0,y2-y0)
      qh = phase(x2-x1,y2-y1) - 0.5*pai
      pp1 = ph1 - pai
      pp2 = ph1 + pai
      if( ph2 .lt. pp1 ) ph2 = ph2 + yen
      if( ph2 .gt. pp2 ) ph2 = ph2 - yen
      if( abs(sin(ph2-ph1)) .lt. 0.0001 ) go to 100
c      ----- nn : division number -----
      nn = 16
      if( abs( ph2-ph1 ) .gt. 0.25*pai ) nn = 31

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if( abs( ph2-ph1 ) .gt. 0.50*pai )  nn = 51
c      -----
      dh = ( ph2 - ph1 ) / float(nn-1)
do 1  m = 1,nn
      phm = ph1 + float(m-1)*dh
      r = r1 * cos(ph1-qh) / cos(phm-qh)
      ra = abs( r / aa )
      ab = abs( ra + sqrt( ra*ra + 1.0 ) )
      alg = alog( ab )
      sg = 1.0
      if( m .eq. 1 .or. m .eq. nn )  sg = 0.5
c      tt = tt  +  sg * dh * r * sin(phm)
      tt = tt  +  sg * dh * aa * alg * sin(phm)
1 continue
      go to 200
100 tt = 0.
200 continue
      sal = 2.0 * tt * gg
      return
      end
c      *-*-*-*-*-*-*-*-*-*-*-*
      function  phase(px,py)
      pai = 3.141593
      if( px .ne. 0. .and. py .ne. 0. )  go to 1
      if( py .eq. 0. .and. px .ge. 0. )  ph = 0.
      if( py .eq. 0. .and. px .lt. 0. )  ph = pai
      if( px .eq. 0. .and. py .gt. 0. )  ph = 0.5 * pai
      if( px .eq. 0. .and. py .lt. 0. )  ph = 1.5 * pai
      go to 6
1 ph = atan(py/px)
      if( px .lt. 0. )  ph = ph + pai
      if( px .gt. 0. .and. py .lt. 0. )  ph = ph + 2.0*pai
6 phase = ph
      return
      end
c      *****

```

```

        subroutine trend(ipol,it)
        common /equ/p(6,7),pn(6),q(6)
        common /gc/gc(500)
        common /go/go(500)
        common /to/to(500)
        common /rg/rg(500)
        common /ite/iobs
        common /xo/xo(500)/xc/xc(500)
        if( ipol.ge.0 .and. ipol.le.5 ) go to 100
        write(6,600)
600 format(1h0,' the value of ipol is exceptional. ')
        go to 110
100 continue
        call kyoku(xo,iobs,omin,omax)
        rng = 3.*(omax-omin)/float(iobs)
c -----
        jpol = ipol + 1
        do 1 i=1,6
        pn(i) = 0.
        do 1 j=1,6
1 p(i,j) = 0.
c >-----
        do 2 i=1,iobs
        x = xo(i)
        sa = go(i) - ( gc(i) + rg(i) )
        q(1) = 1.
        if( ipol .eq. 0 ) go to 4
        do 3 k=1,ipol
3 q(k+1) = x*q(k)
4 continue
c - - - - -
        do 5 l=1,jpol
        pn(l) = pn(l) + sa*q(l)
        do 5 j=1,jpol
5 p(l,j) = p(l,j) + q(l)*q(j)
2 continue

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```

c   <------
      call matrix(jpol)
      write(6,603) (pn(i),i=1,6)
603 format(1h0,'trend : a(0)=' ,e12.3,3x,'a(1)=' ,e12.3,3x,
/           'a(2)=' ,e12.3,3x/
/      1h , '           a(3)=' ,e12.3,3x,'a(4)=' ,e12.3,3x,
/           'a(5)=' ,e12.3)
      do 6 i=1,iobs
x = xo(i)
q(1) = 1.
      if( ipol .eq. 0 ) go to 8
      do 7 k=1,ipol
7 q(k+1) = x*q(k)
8 continue
      gx = 0.
      do 9 j=1,jpol
9 gx = gx + pn(j)*q(j)
      to(i) = gx + rg(i)
      if(it .eq. 1) gc(i) = gc(i) + to(i)
6 continue
110 return
      end
c   *****
      subroutine matrix(iv)
common /equ/p(6,7),pp(6),q(6)
dimension m(6)
ih = iv + 1
      do 41 i=1,iv
m(i)=i
41 continue
      do 15 i=1,iv
p(i,ih) = pp(i)
15 continue
      do 1 i=1,iv
      if( p(i,i).ne.0. ) go to 5
do 6 j=i,iv

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    if( p(j,i).ne.0. ) go to 8
6 continue
    go to 12
8  do 7 k=1,ih
    b = p(j,k)
    p(j,k) = p(i,k)
    p(i,k) = b
7 continue
    go to 5
12 do 9 j=i,iv
    if( p(i,j).ne.0. ) go to 10
9 continue
    go to 13
10 ic = m(i)
    m(i) = m(j)
    m(j) = ic
    do 11 k=1,iv
    b = p(k,j)
    p(k,j) = p(k,i)
    p(k,i) = b
11 continue
5 w = p(i,i)
    do 2 j=1,ih
    p(i,j) = p(i,j)/w
2 continue
    do 3 k=1,iv
    if( k.eq.i ) go to 3
    s = p(k,i)
    do 4 l=1,ih
    p(k,l) = p(k,l) - s*p(i,l)
4 continue
3 continue
1 continue
    do 51 i=1,iv
    ip = m(i)
    pp(ip) = p(i,ih)

```



```

51 continue
   go to 14
13 continue
   write(6,600)
600 format(1h,'matrix : calculation is impossible.')
14 continue
   return
   end
c   *****
   subroutine   stadev(m,gc,go)
   dimension   gc(1)
   dimension   go(1)
   dimension   gs(500)
   su = 0.
   do 1 i=1,m
   s = gc(i) - go(i)
1 su = su + s
   sa = su/float(m)
   do 2 i=1,m
2 gs(i) = gc(i) - sa
   su = 0.
   do 3 i=1,m
   s = gs(i) - go(i)
3 su = su + s*s
   su = su/float(m-1)
   sd =sqrt(su)
   write(6,600) sa,sd
   write(30,600) sa,sd
600 format(1h,'stadev : mean difference   =',f12.5/
/      1h,'      : standard deviation =',f12.5)
   return
   end
c   *****
   subroutine   kyoku(a,m,rmin,rmax)
   dimension   a(1)
   rmin = a(1)

```

```

rmax = a(1)
do 1 i=1,m
  ad = a(i)
  if( ad .lt. rmax ) go to 2
  rmax = ad
  go to 1
2 if( ad .gt. rmin ) go to 1
  rmin = ad
1 continue
return
end

```

```

c *****
subroutine gxysa(xor,xen,gmin,gmax,smin,smax)
common /ite/m
common /gc/gc(500)/go/go(500)/to/to(500)
common /xo/xo(500)/yo/h(500)
  call kyoku(xo,m,omin,omax)
xor = omin
xen = omax
  call kyoku(h,m,hmin,hmax)
smin = hmin
smax = hmax
  call kyoku(go,m,omin,omax)
  call kyoku(gc,m,cmin,cmax)
  call kyoku(to,m,tmin,tmax)
gmin = amin1(omin,cmin,tmin)
gmax = amax1(omax,cmax,tmax)
return
end

```

```

c *****
subroutine glxymm(xlor,xlen,glmin,glmax,slmin,slmax)
  common /ite/m
  common /lay/lay,lpnt(20),dnl(20),lex(20)
common /gl/gl(500,2)
common /xl/xl(500,2)
common /yl/yl(500,2)

```

```

dimension a(500)
      if( lay .eq. 0 ) go to 10
      do 1 l=1,lay
call chg2(gl,l,a)
call kyoku(a,m,amin,amax)
if( lay .eq. 1 ) glmin = amin
if( lay .eq. 1 ) glmax = amax
if( amin .lt. glmin ) glmin = amin
if( amax .gt. glmax ) glmax = amax
1 continue
10      continue
      call tpbtl(xl,xlor,xlen)
      call tpbtl(yl,slmin,slmax)
return
end
c      *****
      subroutine tpbtl(gl,glmin,glmax)
      common /lay/lay,lpnt(20),dnl(20),lex(20)
      dimension gl(500,20),a(500)
if( lay .eq. 0 ) go to 10
      do 1 l=1,lay
call chg2(gl,l,a)
jpnt = lpnt(l)
call kyoku(a,jpnt,amin,amax)
if( lay .eq. 1 ) glmin = amin
if( lay .eq. 1 ) glmax = amax
if( amin .lt. glmin ) glmin = amin
if( amax .gt. glmax ) glmax = amax
1 continue
10 continue
      return
      end
c      *****
      subroutine chg1(a,b)
dimension a(500),b(500)
      do 1 i=1,500

```

```
1 b(i) = a(i)
```

```
   return
```

```
   end
```

```
c *****
```

```
   subroutine chg2(a,m,b)
```

```
   dimension a(500,20),b(500)
```

```
   do 1 i=1,500
```

```
1 b(i) = a(i,m)
```

```
   return
```

```
   end
```

```
c *****
```

```
   subroutine chg3(a,b,n)
```

```
   dimension a(500),b(500,20)
```

```
   do 1 i=1,500
```

```
1 b(i,n) = a(i)
```

```
   return
```

```
   end
```