

states in the original configuration:

$s_i, \dots$ : symbols on the tape ( $s_0$  is the blank symbol.)  
 H: head state to start the reproduction process  
 NH: non-existence of the head  
 EOT: End of Tape

additional states for self-reproduction:

$s'_i, \dots, s''_i, \dots, H', H'', NH', NH'', EOT', EOT'', EOT''', ERA$

notation:

$Q$  indicates NH or H.

(1)

n\_trans H (NH,  $s_i$ , NH)  $\rightarrow$  H''  
 n\_trans NH (H,  $s_i$ , NH)  $\rightarrow$  NH''  
 n\_trans NH (H,  $s_0$ , EOT)  $\rightarrow$  NH''  
 n\_trans NH (NH'',  $s_0$ , EOT)  $\rightarrow$  NH''  
 n\_trans NH (NH'',  $s_i$ , NH)  $\rightarrow$  NH''  
 n\_trans NH'' (H'',  $s_0$ , EOT)  $\rightarrow$  NH  
 n\_trans NH'' (H'',  $s_i$ , NH)  $\rightarrow$  NH  
 n\_trans NH'' (NH,  $s_i$ , NH)  $\rightarrow$  NH  
 n\_trans NH'' (NH,  $s_0$ , EOT)  $\rightarrow$  NH

(2)

div EOT ( $s_0$ , EOT, NH'')  $\rightarrow$  EOT''  
 L\_trans 1 (EOT'', EOT'')  $\rightarrow$  0  
 div EOT ( $s_0$ , NH, EOT'')  $\rightarrow$  EOT''  
 div EOT'' ( $s_0$ , EOT'', EOT'')  $\rightarrow$  EOT'  
 div EOT'' (EOT'', EOT'', NH)  $\rightarrow$  EOT'  
 div  $s_0$  ( $s_i$ , NH, EOT')  $\rightarrow$   $s'_0$   
 div NH (EOT',  $s_0$ , NH)  $\rightarrow$  NH'  
 div NH (EOT',  $s_0$ , H'')  $\rightarrow$  NH'  
 div  $s_i$  ( $s_j$ , H'',  $s'_k$ )  $\rightarrow$   $s'_i$   
 div  $s_i$  ( $s_j$ , NH,  $s'_k$ )  $\rightarrow$   $s'_i$   
 div NH ( $Q'_i$ ,  $s_j$ , NH)  $\rightarrow$  NH'  
 div NH (NH',  $s_i$ , H'')  $\rightarrow$  NH'  
 div H'' (NH',  $s_i$ , NH)  $\rightarrow$  H'  
 div  $s_i$  (EOT', NH,  $s'_j$ )  $\rightarrow$   $s'_i$   
 div NH ( $Q'_i$ ,  $s_j$ , EOT')  $\rightarrow$  NH'  
 com 0 (EOT',  $s'_0$ )  $\rightarrow$  1  
 com 0 (EOT', NH')  $\rightarrow$  1  
 com 0 ( $s'_i$ ,  $s'_j$ )  $\rightarrow$  1  
 com 0 ( $Q'_i$ ,  $Q'_j$ )  $\rightarrow$  1  
 n\_trans EOT'' (EOT', EOT', EOT'')  $\rightarrow$  EOT''  
 n\_trans EOT'' (EOT', EOT', EOT'')  $\rightarrow$  EOT''  
 com 0 (EOT'', EOT'')  $\rightarrow$  1  
 ann 1 (EOT'', EOT'')  $\rightarrow$   $\phi$   
 n\_trans  $s'_0$  ( $s'_0$ , NH', EOT')  $\rightarrow$  NH  
 n\_trans  $s'_i$  ( $s'_i$ ,  $Q'_k$ ,  $s'_j$ )  $\rightarrow$   $Q_k$   
 n\_trans  $Q'_i$  ( $Q'_i$ ,  $s'_j$ ,  $Q'_k$ )  $\rightarrow$   $s''_j$

n\_trans NH' (NH',  $s'_0$ , EOT')  $\rightarrow$   $s''_0$   
 n\_trans EOT' (EOT',  $s'_0$ , NH)  $\rightarrow$  NH  
 n\_trans NH ( $s'_0$ ,  $s''_0$ , EOT')  $\rightarrow$  ERA  
 n\_trans  $s'_i$  (ERA,  $s'_j$ , NH)  $\rightarrow$  NH  
 n\_trans  $s'_j$  (ERA,  $s'_j$ , H)  $\rightarrow$  H''  
 n\_trans  $Q_i$  ( $s'_j$ ,  $s''_j$ ,  $s'_k$ )  $\rightarrow$  ERA  
 n\_trans EOT' (EOT', NH',  $s''_0$ )  $\rightarrow$   $s_0$   
 n\_trans  $s''_0$  (NH', NH, EOT')  $\rightarrow$  ERA  
 n\_trans  $Q'_i$  ( $s_j$ ,  $Q'_k$ ,  $s''_l$ )  $\rightarrow$   $s_l$   
 n\_trans  $s''_i$  ( $q'_j$ , ERA,  $s_k$ )  $\rightarrow$  ERA  
 ann 0 (ERA, ERA)  $\rightarrow$   $\phi$   
 ann 1 (ERA, ERA)  $\rightarrow$   $\phi$   
 n\_trans  $s'_0$  ( $s'_i$ , NH, EOT')  $\rightarrow$   $s_0$   
 n\_trans  $s'_i$  ( $s'_j$ , NH,  $s_k$ )  $\rightarrow$   $s_i$   
 n\_trans  $s'_i$  ( $s'_j$ , H'',  $s_k$ )  $\rightarrow$   $s_i$   
 n\_trans  $s'_0$  (EOT', NH,  $s_i$ )  $\rightarrow$   $s_0$   
 l\_trans 1 ( $s_i$ ,  $s_j$ )  $\rightarrow$  0  
 l\_trans 1 ( $s_i$ ,  $Q_j$ )  $\rightarrow$  0  
 (3)  
 n\_trans EOT' (EOT',  $s'_0$ ,  $s_0$ )  $\rightarrow$  ERA  
 n\_trans  $s'_0$  (NH, ERA, EOT')  $\rightarrow$  ERA  
 n\_trans EOT' (EOT', EOT', ERA)  $\rightarrow$  EOT  
 n\_trans EOT' (EOT, EOT', NH)  $\rightarrow$  ERA  
 n\_trans EOT' ( $s_0$ , ERA, EOT')  $\rightarrow$  ERA  
 n\_trans EOT' (NH',  $s_0$ , EOT')  $\rightarrow$  EOT  
 n\_trans NH' ( $Q'_i$ ,  $s_0$ , EOT)  $\rightarrow$  NH  
 n\_trans NH' ( $Q'_i$ ,  $s_j$ , NH)  $\rightarrow$  NH  
 n\_trans NH' ( $Q'_j$ ,  $s_j$ , EOT'')  $\rightarrow$  NH  
 n\_trans H' (NH,  $s_i$ , NH)  $\rightarrow$  EOT''  
 n\_trans EOT'' (NH,  $s_i$ , NH)  $\rightarrow$  H''  
 n\_trans NH' (EOT',  $s_0$ , NH)  $\rightarrow$  NH  
 n\_trans NH' (EOT',  $s_0$ , EOT'')  $\rightarrow$  NH  
 n\_trans EOT' ( $s_0$ , EOT', EOT)  $\rightarrow$  EOT''  
 n\_trans EOT' (NH, EOT', EOT'')  $\rightarrow$  ERA  
 n\_trans EOT' (EOT', NH', NH)  $\rightarrow$  ERA  
 n\_trans NH' ( $s_0$ , ERA, EOT')  $\rightarrow$  ERA  
 n\_trans EOT' (EOT, EOT', ERA)  $\rightarrow$  EOT''  
 n\_trans EOT' ( $s_0$ , EOT'', ERA)  $\rightarrow$  ERA  
 l\_trans 1 ( $Q_i$ ,  $Q_j$ )  $\rightarrow$  0  
 l\_trans 1 (EOT,  $s_0$ )  $\rightarrow$  0  
 l\_trans 1 (EOT, NH)  $\rightarrow$  0  
 (4)  
 n\_trans EOT'' ( $s_0$ , NH, EOT)  $\rightarrow$  EOT'  
 n\_trans EOT' (EOT,  $s_0$ , NH)  $\rightarrow$  EOT  
 n\_trans NH (EOT',  $s_0$ , NH)  $\rightarrow$  NH''  
 n\_trans NH (EOT',  $s_0$ , H'')  $\rightarrow$  NH''  
 n\_trans NH'' (EOT,  $s_0$ , NH)  $\rightarrow$  NH  
 n\_trans NH'' (EOT,  $s_0$ , H'')  $\rightarrow$  NH  
 n\_trans NH (NH'',  $s_i$ , H'')  $\rightarrow$  NH''  
 n\_trans NH'' (NH,  $s_i$ , H'')  $\rightarrow$  NH  
 n\_trans H'' (NH'',  $s_i$ , NH)  $\rightarrow$  H