

Superconductivity and stripes in 2D electronic model

Electrotechnical Laboratory

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1. Introduction

d-p model stripes

high-T_c superconductor

2. Method and Calculations

3. Stripes and Phase diagram

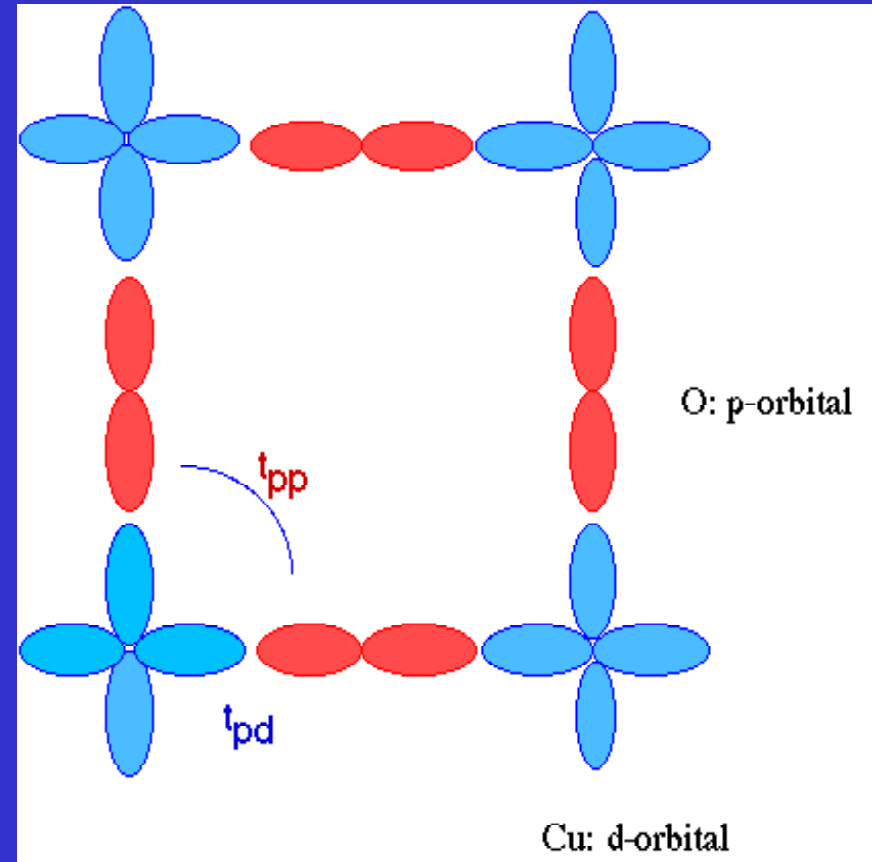
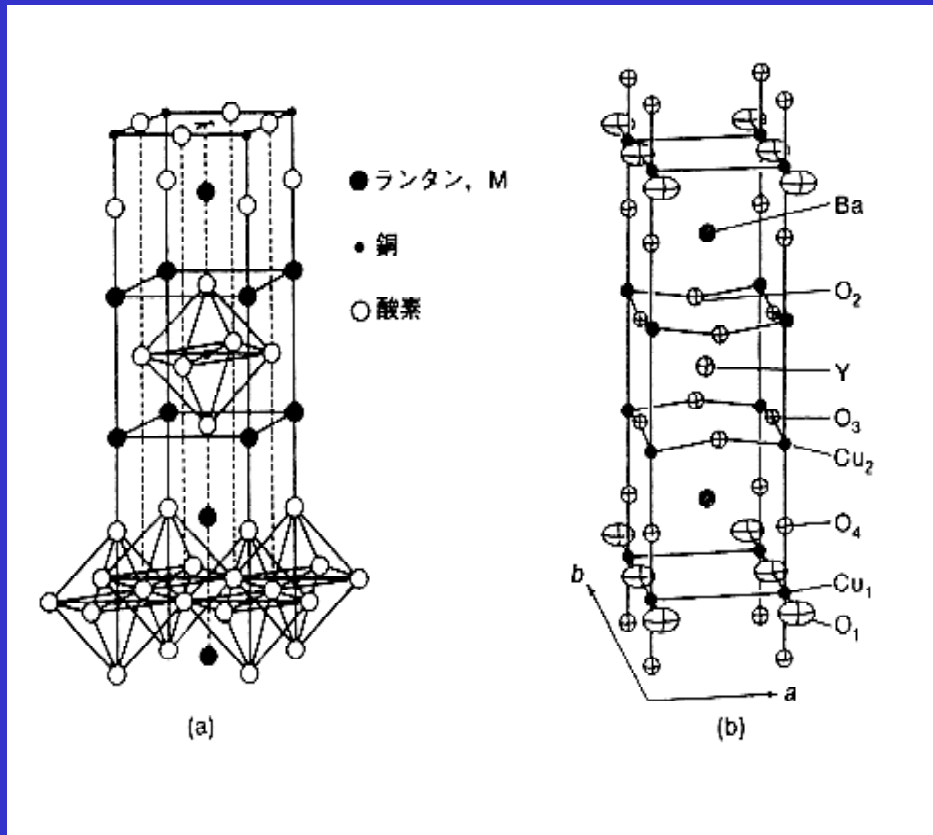
Condensation energy

4. Summary

Introduction

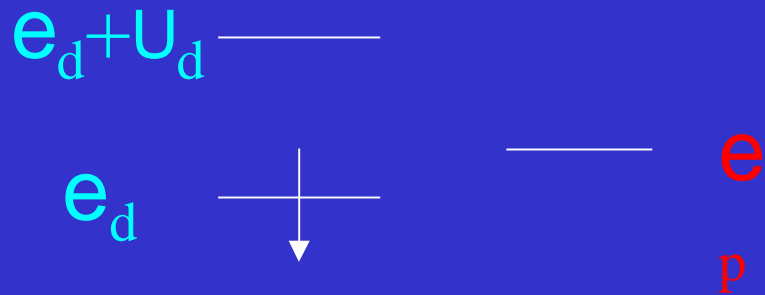
High-Tc cuprates

CuO₂ plane 2D d-p model



2D Cu-O model

Non-doping (half-filling)

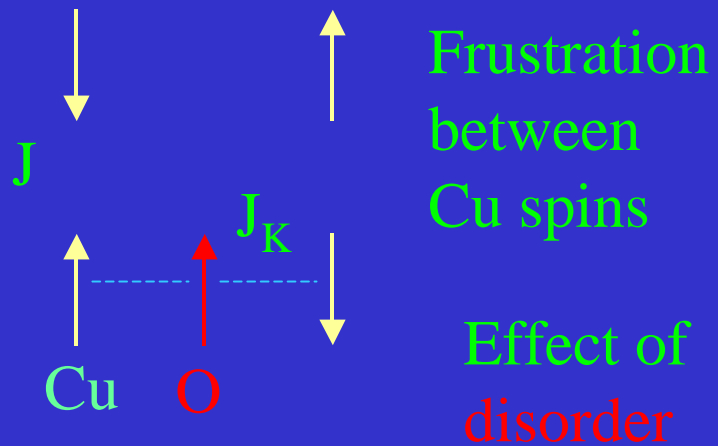


Antiferromagnetic Insulator

Hole doping

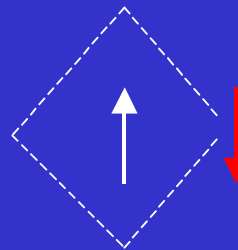
Hole is doped on O site.

1. Frustration



2. Local singlet (Zhang-Rice)

Singlet

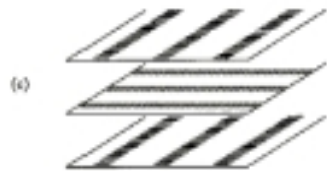
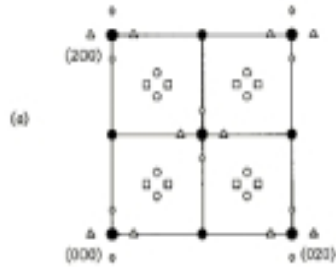


Hubbard model
t-J model

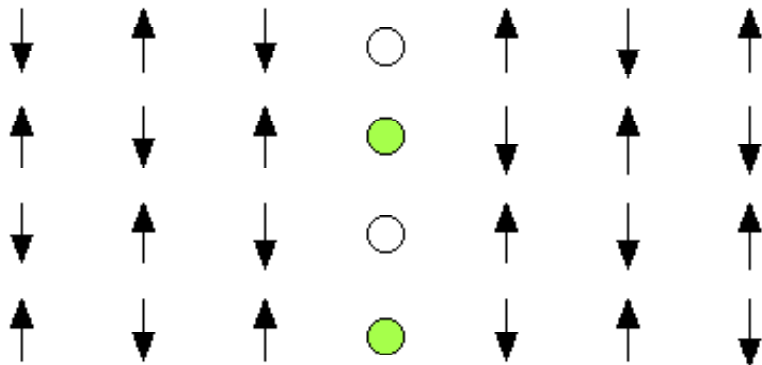
Characteristics of HTSC

	LaSrCuO	YBaCuO	BiSrCaCuO	NdCeCuO
d-wave pairing	●	●	●	○
Pseudogap		●	●	
Incom. peaks	●	●		
Resonance peaks		●	●	
Stripes	●			

Stripes in High-Tc cuprates



Incommensurate structure



Proposal of Stripes

$\text{La}_{2-x-y}\text{Nd}_y\text{Sr}_x\text{CuO}_4$
Tranquada et al.

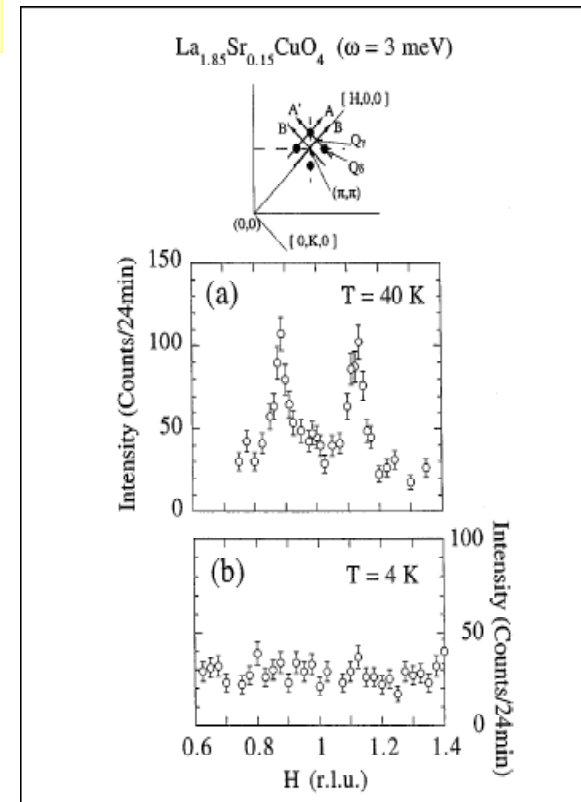
Phys. Rev. B54,4596('96)

Two Q vectors

$$Q_s = (\pi - 2\pi\delta, \pi), \dots$$

$$Q_c = (4\pi\delta, 0), \dots$$

Incommensurate peaks



Yamada et al.
Phys. Rev. B

Method and Calculations

Variational Monte Carlo method

Wave functions

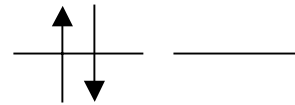
$$\Psi_N = P_G |\text{Fermi sea})$$

$$\Psi_{\text{BCS}} = P_G |\text{BCS})$$

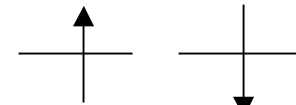
$$\Psi_{\text{SDW}} = P_G |\text{SDW})$$

Gutzwiller Projection P_G

To control the on-site strong correlation



Weight g
Coulomb $+U$



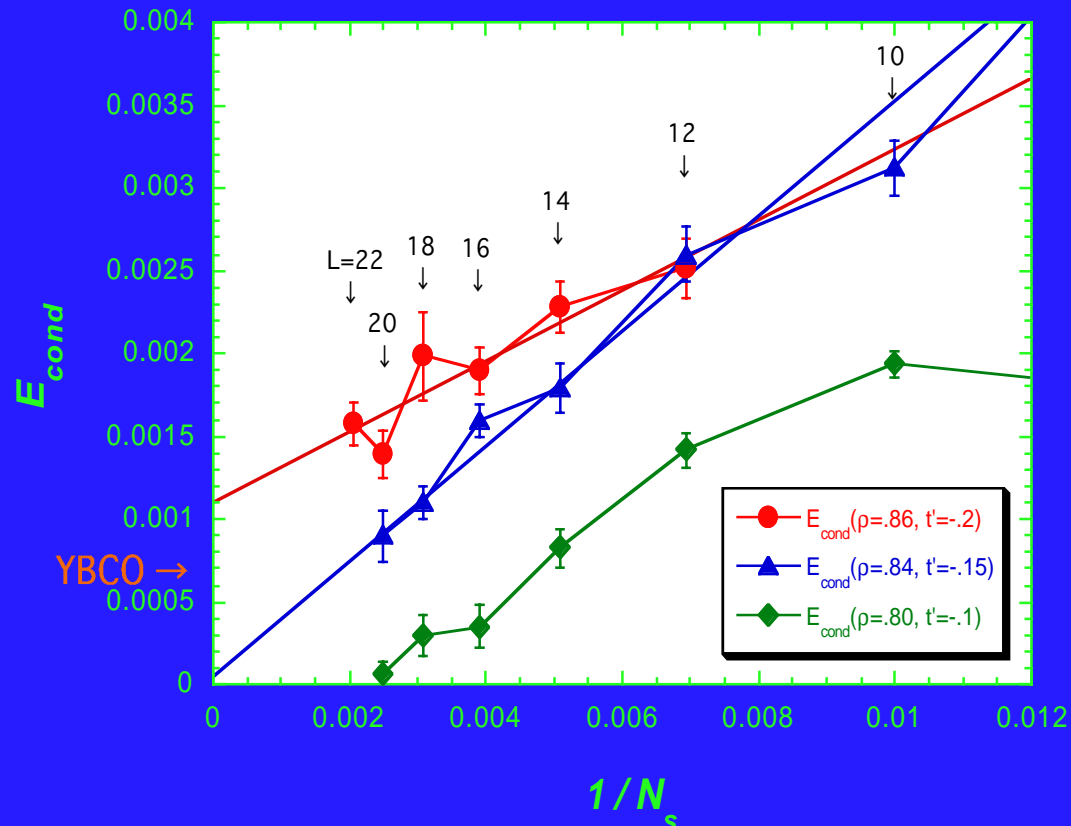
Weight 1
Parameter $0 < g < 1$

P_G induces antiferromagnetic correlation

SC Condensation Energy

2D Hubbard model

Bulk Limit of SC E_{cond} of 2D Hubbard Model ($U=8$)



Ref. Physica C304 (1998) 225

Bulk limit

$$E_{\text{cond}} = 0.00117t$$

$$= 0.59 \text{ meV/site}$$

($\rho=0.86, t'=-0.2, U=8$)

Experiments

0.26 meV/site

(Critical H_c

0.17~0.26 (C/T)

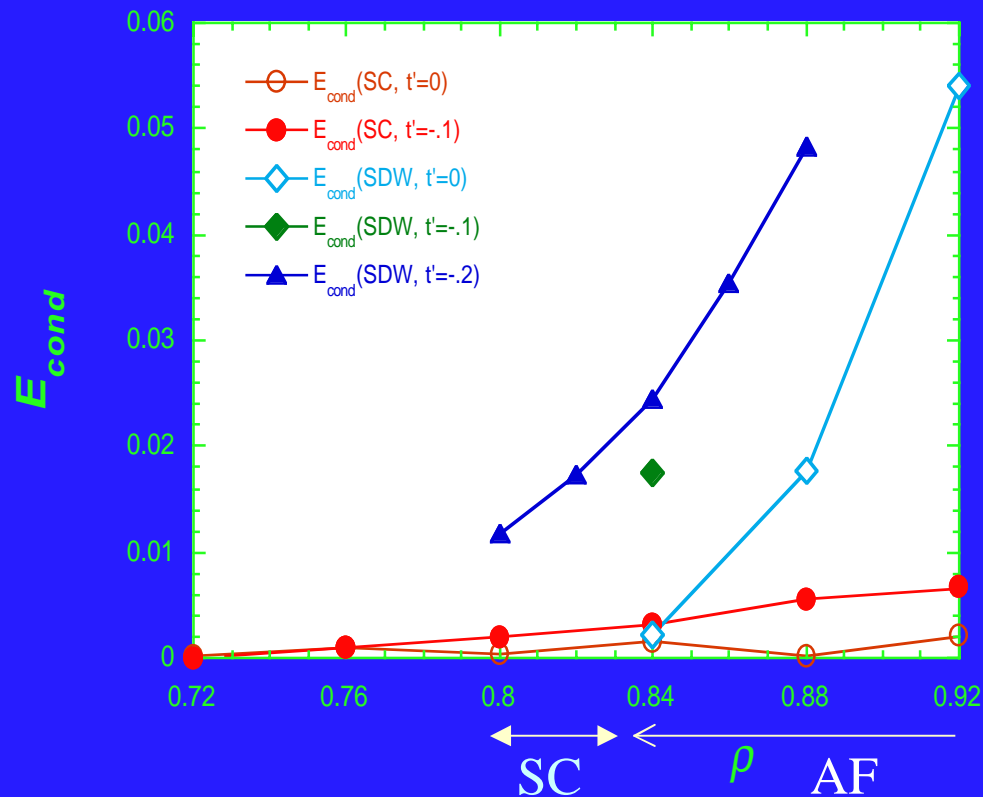
They agree very well.

t-J model gives 50 times
of condensation energy !

Competition between SC and AF

Energy gains of SC and AF states

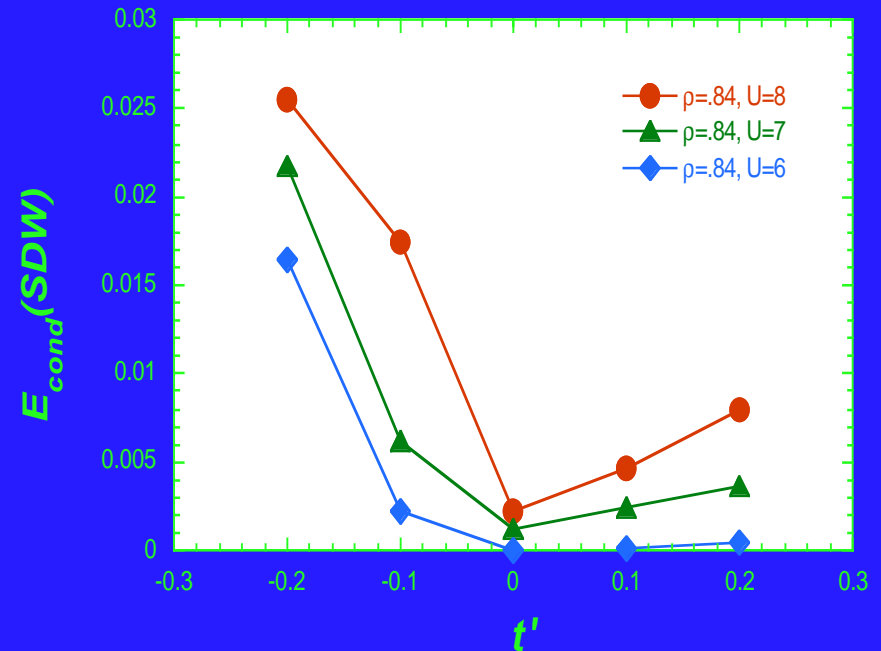
$E_{\text{cond}}(\text{SC, SDW})$ vs ρ $U=8$ 10×10



Important factors for SC

- Next n.n. transfer
- Correlation between neighboring sites
- Strength of the Coulomb repulsion

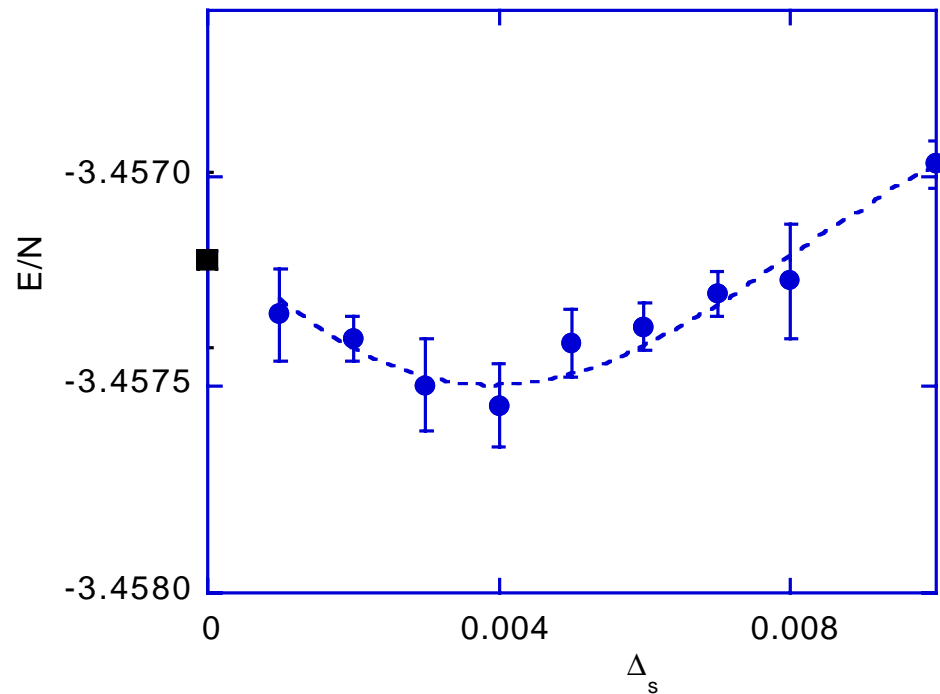
t' dependence of $E_{\text{cond}}(\text{SDW}, \rho=.84, 10 \times 10)$



Coexistence of uniform AF and SC

Gutzwiller wave function with SC and AF order parameters

VMC results



6x6

$d = 0.111$

$U_d = 8$

SC order parameter

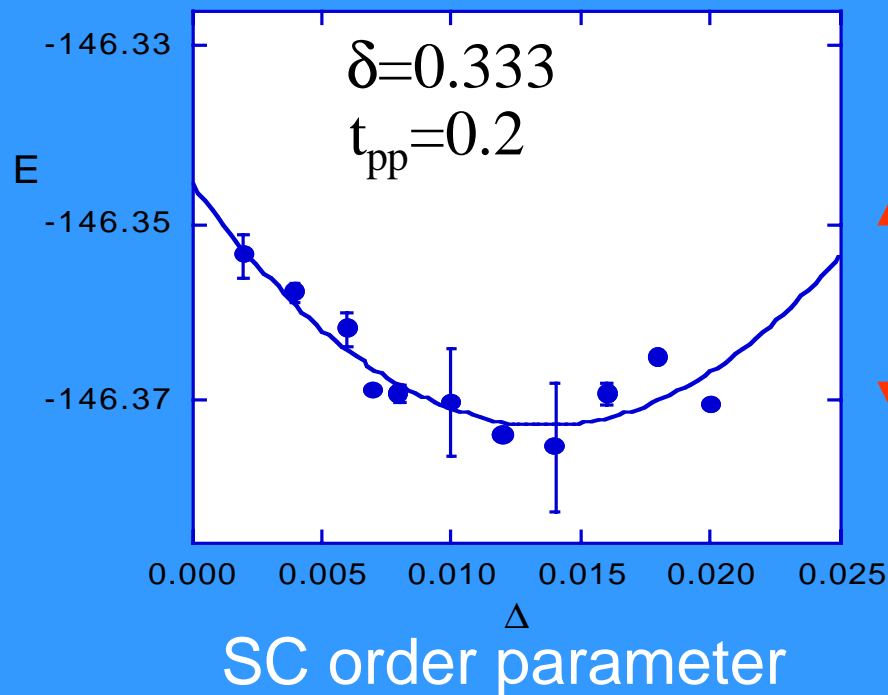
Phase diagram of d-p model

Condensation energy

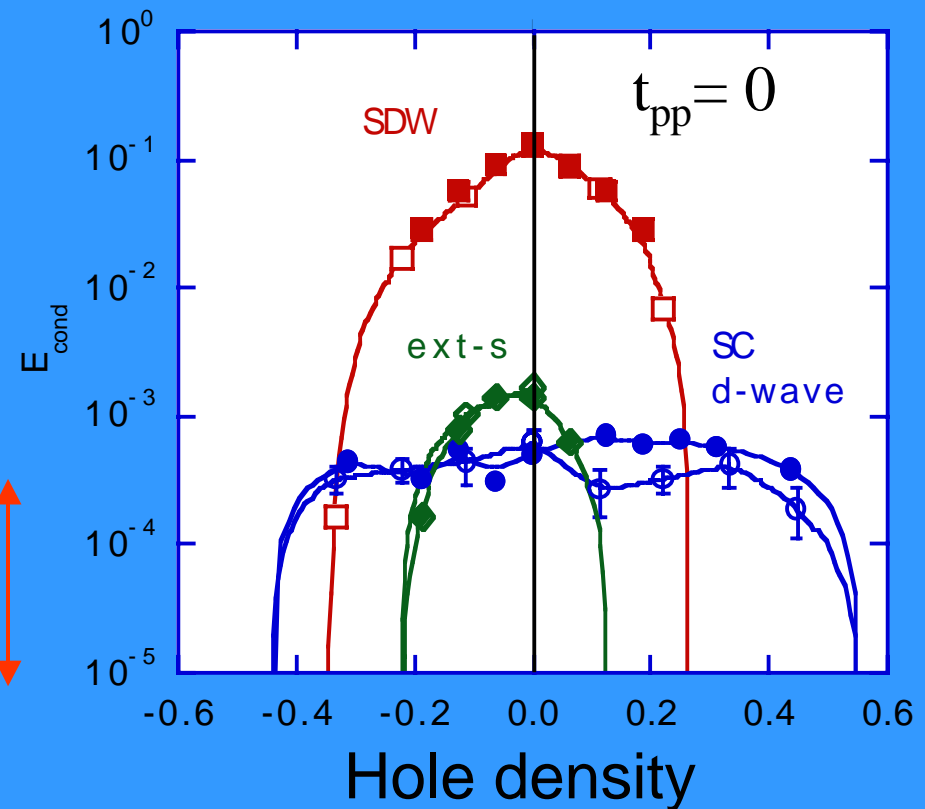
$$E_{\text{cond}} \sim 0.00038 t_{\text{dp}} \\ = 0.56 \text{ meV/site}$$

Specific heat ~ 0.26

Agreement is excellent!



2D d-p model 6x6 and 8x8



Ref. Phys. Rev. B64, 184509 (2001)

Wave functions for Stripes

SDW potential

$$H_{AF} = \frac{U}{2} \sum_{i,\sigma} [n_i - \sigma(-1)^{x_i+y_i} m_i] c_{i,\sigma}^\dagger c_{i,\sigma} \quad \text{d electron part}$$

$$n_i = 1 - \alpha / \cosh[(y_i - y_1) / \xi_\rho] - \alpha / \cosh[(y_i - y_2) / \xi_\rho]$$

$$m_i = m \tanh[(y_i - y_1) / \xi_\sigma] \tanh[(y_i - y_2) / \xi_\sigma] .$$

(2-stripe case)

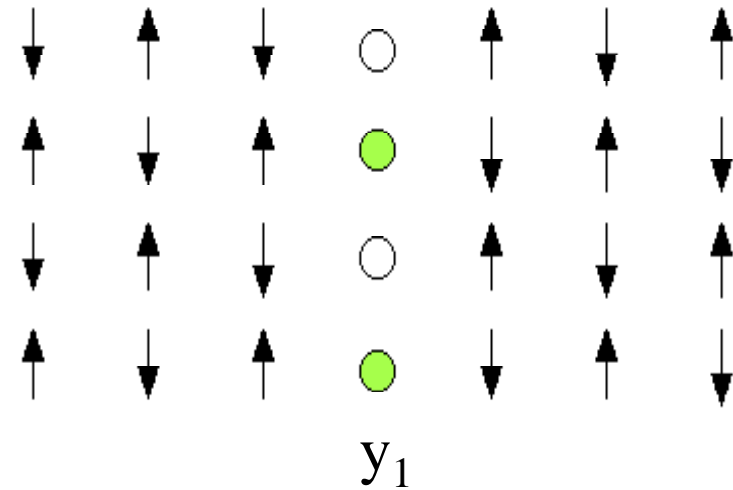
or

$$n_i \sim -a \cos(4pdy_i)$$

$$m_i = m \cos(2pdy_i)$$

Giamarchi et al.
Phys. Rev. B43, 12943 ('91)

Stripe



Gutzwiller function

$$\Psi = P_G \Psi_{\text{stripe}}$$

Non-uniform Spin-density wave

What spin structures are stable?

It depends on parameters in d-p model

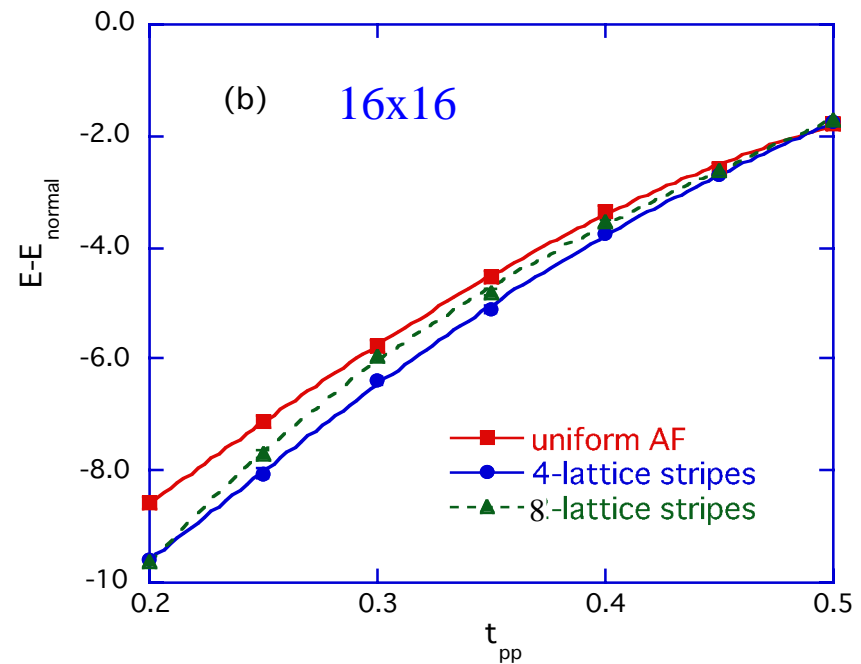
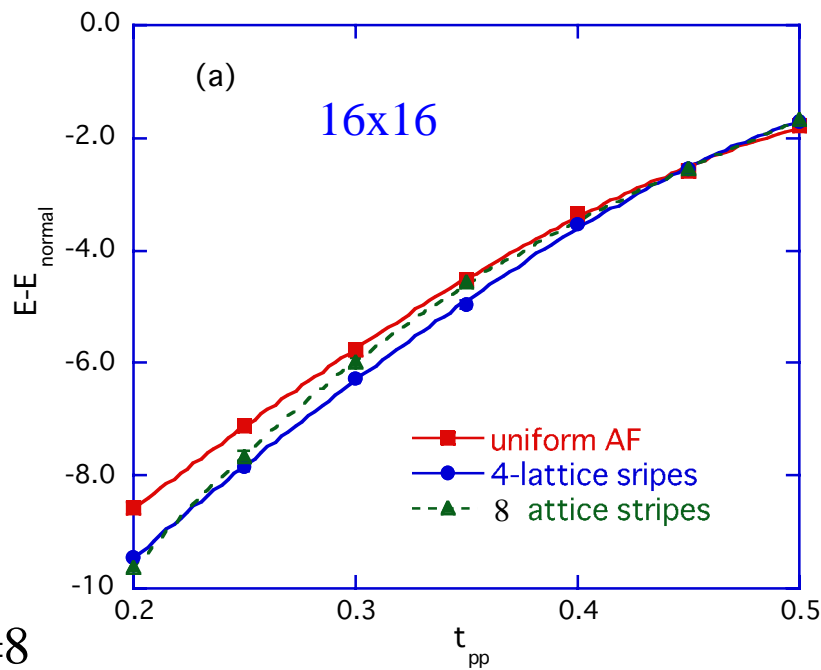
$$t_{pp}, \Delta = \epsilon_p - \epsilon_d$$

Long-period stripes

Uniform SDW

Stripes with short periods

Uniform distributions of holes



$$U_d=8$$

$$\Delta=2$$

Antiperiodic-periodic b.c.s

Periodic-antiperiodic b.c.s

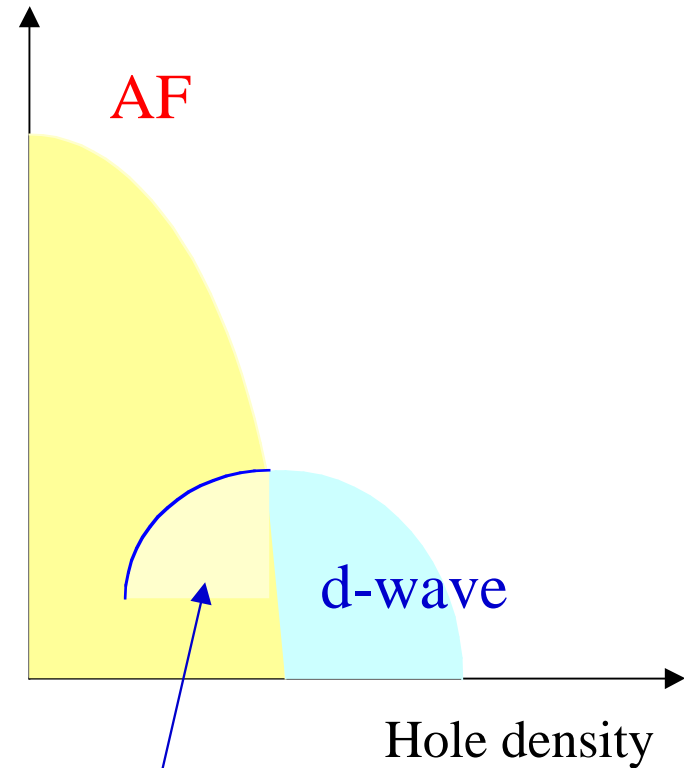
Summary

2D Hubbard model (single-band and three-band)

- Overdoped region
d-wave SC originating from U

- Underdoped region
Antiferromagnetism
= Non-uniform SDW (Stripes)

Coexistent of SC and AF (stripes)



AF (stripes) and SC
can coexist.